MIT 6.035 Spring 2011 Quiz 1 (100 points)

Your Full Name Here:

Your Athena ID Here:

1. (5 points) Write a regular expression for the language $\mathrm{L}=\left\{0^{\mathrm{n}} 1^{\mathrm{m}} \mid(\mathrm{n}+\mathrm{m})\right.$ is even $\}$.
2. (20 points) Let the alphabet $\sum=\{0,1\}$.
(a) (5 points) Write a regular expression for the language of all strings over $\sum$ that contain the contiguous substring 11 .
(b) (5 points) Write a regular expression for the language of all strings over $\sum$ that do not contain the contiguous substring 11 .
(c) (5 points) Give a non-deterministic finite automaton (NFA) for the language of all strings over $\sum$ that contain the contiguous substring 11 .
(d) (5 points) Give a non-deterministic finite automaton (NFA) for the language of all strings over $\sum$ that don't contain the contiguous substring 11 .
3. (10 points)
(a) (5 points) Give a non-deterministic finite automaton (NFA) for the language $\mathrm{L}=(010 \mid 01)^{*}$. The NFA must contain at most 3 states. (Hint: draw an NFA with 4 states, then optimize).
(b) (5 points) Give a deterministic finite automaton for the language $L$.

## 4. (30 points)

Consider the following grammar:
$\mathrm{S} \rightarrow \mathrm{L}=\mathrm{R}$
$\mathrm{L} \rightarrow$ * $\mathrm{R} \mid \mathrm{id}$
$\mathrm{R} \rightarrow \mathrm{L}$
You can think of L and R as standing for l-value and r -value, respectively. * is the dereference operator or indirection operator in C -like languages.

A shift-reduce parser can perform the following sequence of actions to accept the string "*id $=\mathrm{id}$ ".
shift» shift» reduce » reduce » reduce » shift» shift» reduce » reduce » reduce » accept
(a) (10 points) Give a sequence of actions that a shift-reduce parser can take to accept the string "id $=\mathrm{id}$ ".
(b) (10 points) Give a sequence of actions that a shift-reduce parser can take to accept the string "*id = *id".
(c) (10 points) Is the grammar ambiguous? Why or why not?

## 5. (15 points)

Consider the following grammar:

$$
\begin{aligned}
& \mathrm{S} \rightarrow \text { if } \mathrm{E} \text { then } \mathrm{S} \text { else } \mathrm{S} \mid \text { begin } \mathrm{S} L \mid \text { print } \mathrm{E} \mid \varepsilon \\
& \mathrm{L} \rightarrow \text { end } \mid ; \mathrm{S} L \\
& \mathrm{E} \rightarrow \text { num }=\text { num }
\end{aligned}
$$

The goal is to write a recursive-descent parser for the grammar. You are given the following $\mathrm{L}(\mathrm{)}$ ) and E() functions. Your job is to write the $S()$ function on the next page.

```
L() {
    if (token = end) {
        match(end);
        } else if (token = ;) {
            match(;); S(); L();
        } else {
            throw SyntaxError;
            }
}
E() {
    if (token = num) {
        match(num); match(=); match(num);
        } else {
            throw SyntaxError;
        }
}
```

6. (20 points)

The following is a code snippet of legal-01.dcf:

```
class Program {
    int A[100];
    int length;
    void main() {
            int temp;
            length = 100;
            callout("srandom", 17);
            for i = 0, length {
                temp = callout("random");
                A[i] = temp;
            }
        /* <HERE> */
    }
}
```

What should the symbol tables look like at <HERE>, considering the semantics of the Decaf language?
Complete the symbol tables on the next page in the similar way to the symbol tables presented at Lecture 5. (Hint: note that the Decaf language is different from the language presented at Lecture 5).


